

## Experimental and Theoretical Study of the Vibrational Spectra of 12-Crown-4–Alkali Metal Cation Complexes

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The vibrational, Raman, and IR, spectra of the five 12-crown-4 (12c4) complexes with Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup>, Rb<sup>+</sup>, and Cs<sup>+</sup> alkali metal cations were measured. Except for a small shift of the position of some bands in the vibrational spectra of the Li<sup>+</sup> complex, the vibrational spectra of the five complexes are so similar that it is concluded that the five complexes exist in the same conformation. B3LYP/6-31+G\* force fields were calculated for six of the eight predicted conformations in a previous report (*J. Phys. Chem. A* 2005, 109, 8041) of the 12c4–Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> complexes that are of symmetries higher than the C<sub>1</sub> symmetry. These six conformations, in energy order, are of C<sub>4</sub>, C<sub>s</sub>, C<sub>s</sub>, C<sub>2v</sub>, C<sub>2v</sub>, and C<sub>s</sub> symmetries. Comparison between the experimental and calculated vibrational frequencies assuming any of the above-mentioned six conformations shows that the five complexes exist in the C<sub>4</sub> conformation. This agrees with the fact that the five alkali metal cations are larger than the 12c4 ring cavity. The B3LYP/6-31+G\* force fields of the C<sub>4</sub> conformation of the Li<sup>+</sup>, Na<sup>+</sup> and K<sup>+</sup> complexes were scaled using a set of eight scale factors and the scale factors were varied so as to minimize the difference between the calculated and experimental vibrational frequencies. The root-mean-square (rms) deviations of the calculated frequencies from the experimental frequencies were 7.7, 5.6, and 5.1 cm<sup>-1</sup> for the Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> complexes, respectively. To account for the earlier results of the Li<sup>+</sup> complex that the C<sub>s</sub> conformation is more stable than the C<sub>4</sub> conformation by 0.16 kcal/mol at the MP2/6-31+G\* level, optimized geometries of the complex were calculated for the C<sub>4</sub> and C<sub>s</sub> conformations at the MP2/6-311++G\*\* level. The C<sub>4</sub> conformation was calculated to be more stable than the C<sub>s</sub> conformation by 0.13 kcal/mol.

### Introduction

Recently there has been a wide interest shown in the chemistry of crown ethers. This interest is due to the ability of crown ethers to form strong complexes with ionic species, especially alkali metal cations, with high selectivity. Consequently, crown ethers have found a large number of industrial and medical applications. Crown ethers are used in nuclear waste disposal,<sup>1–5</sup> membrane transport,<sup>6–8</sup> anion activation,<sup>9,10</sup> formation of soluble and insoluble polymers,<sup>11–14</sup> and macrocyclic liquid crystals.<sup>15</sup>

Because of the importance of the applications of crown ethers, our objective was set to study this class of molecules to determine in which conformation, or conformations, these large ring flexible molecules exist in. The methodology we use to achieve this goal is through the conformational analysis and vibrational study of free crown ethers and some of their complexes. Although our attention was attracted first to the most important crown ether, 18-crown-6 (18c6), due to its large size, our effort was turned to the smaller and easier to study 12c4.

In a previous report,<sup>16</sup> a full conformational search of the possible conformations of free 12c4 was performed at the MM3 level. The search was performed using an efficient method of conformational search of cyclic molecules, the CONFLEX method.<sup>17–20</sup> The method, as implemented in the CAChe

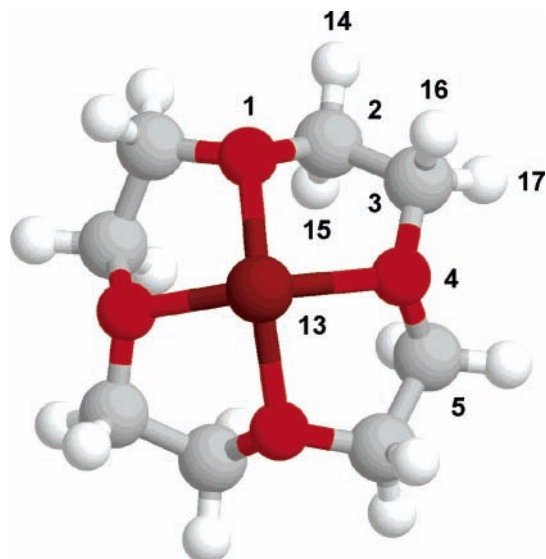
program,<sup>21</sup> has the advantage of being fully programmed. This minimizes the human interference and consequently minimizes human error. This is compared to other conformational search methods that can be termed as half programmed–half manual. The conformational search of 12c4 resulted in the prediction of 180 conformations. Energy order of the predicted conformations was calculated at levels of theory as high as the MP2/6-31+G\* level. Similar to previous reports,<sup>22–24</sup> the study predicted that the S<sub>4</sub> conformation is the lowest energy conformation of 12c4. At the MP2/6-31+G\* level, the S<sub>4</sub> conformation is more stable than the C<sub>i</sub> conformation by 2.61 kcal/mol. In a following vibrational study of free, or rather uncomplexed, 12c4, it was shown for the first time that 12c4 in the solid, liquid, and considered solution phases exists in the C<sub>i</sub> conformation.<sup>25</sup> The case is similar for the larger 18c6. It is known experimentally, using the vibrational spectra<sup>26,27</sup> and X-ray,<sup>28,29</sup> that 18c6 exists in the C<sub>i</sub> conformation. A similar conformational search, as that performed for 12c4, predicted for the first time that the lowest energy conformation of free 18c6 is a S<sub>6</sub> conformation. At the MP2/6-31+G\* level, the S<sub>6</sub> conformation is more stable than the experimentally known C<sub>i</sub> conformation by 1.84 kcal/mol.<sup>30</sup> It was shown that the stability of the lowest energy S<sub>4</sub> conformation of 12c4 and the lowest energy S<sub>6</sub> conformation of 18c6 is due to a combination of both more number of oxygen atoms participating in hydrogen bonding and at distances shorter than that of any of the other conformations.<sup>16,30</sup>

In a continuing study, conformational analysis of 12c4–alkali metal cation complexes was performed.<sup>31</sup> The study predicted eight possible conformations of these complexes. It was

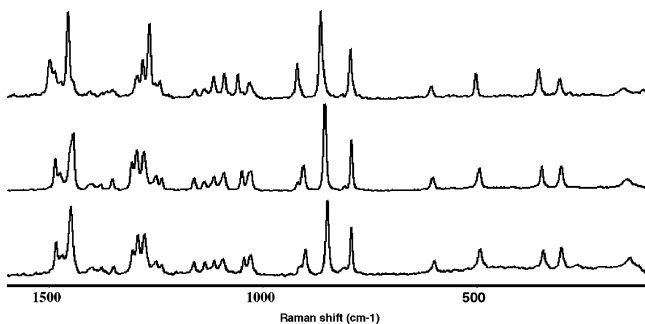
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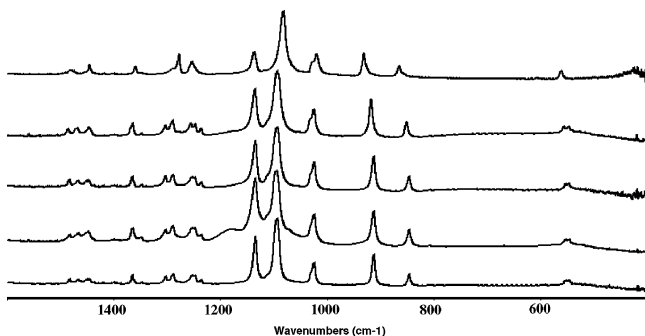
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**Figure 1.** Structure and atom numbering of the  $C_4$  conformation of the 12c4-alkali metal cation complexes.



**Figure 2.** Raman spectra of the solid phase of the three 12c4- $\text{Li}^+$  (top),  $\text{Na}^+$  (middle) and  $\text{K}^+$  (bottom) complexes.



**Figure 3.** IR spectra of the solid phase of the 12c4- $\text{Li}^+$  (top),  $\text{Na}^+$  (second from the top),  $\text{K}^+$  (third from the top),  $\text{Rb}^+$  (fourth from the top) and  $\text{Cs}^+$  (bottom) complexes.

concluded that the  $C_4$  conformation is the lowest energy conformation of the 12c4- $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Rb}^+$  and  $\text{Cs}^+$  complexes. For the 12c4- $\text{Li}^+$  complex, a  $C_s$  conformation is the lowest energy conformation, although, at the MP2/6-31+G\* level, the  $C_4$  conformation is less stable than this  $C_s$  conformation by only 0.16 kcal/mol. The best agreement between the experimental and calculated binding energies is obtained assuming the  $C_4$  or  $C_s$  conformation of the 12c4- $\text{Li}^+$  and  $\text{Na}^+$  complexes and the  $C_4$  conformation of the 12c4- $\text{K}^+$  complex. For the 12c4- $\text{Rb}^+$  and - $\text{Cs}^+$  complexes, poor agreement is obtained between the experimental and calculated binding energies assuming  $C_4$  conformations of both complexes. Instead, the best agreement is obtained assuming a  $C_{2v}$  structure of both complexes. Since this disagrees with the energy order mentioned above, Feller

**TABLE 1: Geometry of the 12c4-Alkali Metal Cation Complexes at the B3LYP/6-31+G\* and MP2/6-31+G\* Levels<sup>a</sup>**

coordinate	$\text{Li}^+$	$\text{Na}^+$	$\text{K}^+$	$\text{Rb}^+$	$\text{Cs}^+$
$\text{O}_1-\text{C}_2$	1.437	1.434	1.431	1.429	1.428
	1.440	1.437	1.433	1.432	1.431
$\text{C}_2-\text{C}_3$	1.524	1.525	1.524	1.525	1.525
	1.516	1.517	1.516	1.516	1.516
$\text{C}_1-\text{O}_4$	1.440	1.437	1.433	1.431	1.430
	1.444	1.441	1.437	1.435	1.434
$\text{M}-\text{O}$	2.120	2.334	2.747	2.986	3.226
	2.018	2.394	2.708	2.930	3.144
$\text{C}_2-\text{H}_{14}$	1.098	1.099	1.100	1.100	1.101
	1.097	1.099	1.099	1.100	1.100
$\text{C}_2-\text{H}_{15}$	1.099	1.098	1.098	1.098	1.098
	1.099	1.097	1.097	1.097	1.097
$\text{C}_3-\text{H}_{16}$	1.093	1.094	1.095	1.095	1.095
	1.093	1.093	1.094	1.094	1.094
$\text{C}_3-\text{H}_{17}$	1.096	1.097	1.098	1.099	1.099
	1.096	1.098	1.098	1.099	1.099
$\text{O}_1\text{C}_2\text{C}_3$	106.0	107.8	108.5	108.8	108.9
	105.3	107.1	107.3	107.5	107.5
$\text{C}_2\text{C}_3\text{O}_4$	109.0	111.8	112.6	112.9	113.1
	109.4	111.2	111.5	111.8	112.0
$\text{C}_3\text{O}_4\text{C}_5$	116.7	115.9	115.4	115.3	115.3
	115.2	114.4	114.0	113.9	113.9
$\text{MO}_4\text{C}_3$	109.4	109.2	109.9	110.2	110.4
	109.5	110.0	110.8	111.0	111.2
$\text{MO}_4\text{C}_5$	109.1	113.2	118.6	120.8	122.7
	109.2	115.1	119.7	121.9	123.7
$\text{O}_1\text{C}_2\text{H}_{14}$	110.2	110.0	110.0	110.0	110.1
	110.1	109.9	110.1	110.2	110.2
$\text{C}_3\text{C}_2\text{H}_{14}$	110.5	109.7	109.4	109.2	109.2
	111.0	110.2	110.0	109.8	109.8
$\text{O}_1\text{C}_2\text{H}_{15}$	110.2	110.3	110.4	110.4	110.5
	110.2	110.3	110.4	110.5	110.5
$\text{O}_3\text{C}_2\text{H}_{15}$	111.4	111.0	110.7	110.6	110.5
	111.5	111.1	110.9	110.8	110.8
$\text{C}_2\text{C}_3\text{H}_{16}$	110.3	110.1	109.9	109.9	109.8
	110.3	110.1	110.0	109.8	109.8
$\text{O}_4\text{C}_3\text{H}_{16}$	105.7	105.6	105.7	105.7	105.7
	105.6	105.6	105.7	105.7	105.7
$\text{C}_2\text{C}_3\text{H}_{17}$	111.1	110.2	109.8	109.6	109.5
	111.6	110.7	110.5	110.3	110.3
$\text{O}_4\text{C}_3\text{H}_{17}$	111.0	110.7	110.7	110.7	110.8
	110.7	110.5	110.7	110.7	110.7
$\text{O}_1\text{C}_2\text{C}_3\text{O}_4$	-50.9	-56.1	-58.4	-58.9	-59.4
	-52.8	-56.9	-57.9	-58.5	-58.9
$\text{C}_2\text{C}_3\text{O}_4\text{C}_5$	-91.5	-84.0	-81.0	-80.2	-79.7
	-88.8	-83.0	-81.6	-80.8	-80.4
$\text{C}_3\text{O}_4\text{C}_5\text{C}_6$	168.1	164.7	163.5	162.9	162.7
	168.7	165.6	165.0	164.6	164.4
$\text{MO}_1\text{C}_2\text{C}_3$	43.5	37.5	29.9	26.3	23.2
	45.1	36.7	30.5	27.1	24.0

<sup>a</sup> See Figure 1 for atom numbering. Bond lengths in Å and angles in degrees. For each coordinate, the first line corresponds to the B3LYP/6-31+G\* level and the second line corresponds to the MP2/6-31+G\* level. M refers to alkali metal cation.

and co-workers argued that spectral measurement of the binding energy of the 12c4- $\text{Rb}^+$  and - $\text{Cs}^+$  complexes samples both complexes in this high energy  $C_{2v}$  conformation rather than the lowest energy  $C_4$  conformation.<sup>32-37</sup>

Surprisingly, as the number of studies of the vibrational spectra of free 12c4 is quite limited,<sup>38-44</sup> the number of studies of the vibrational spectra of its alkali metal cation complexes, to the best of our knowledge, is very scarce.<sup>38,40</sup> The most detailed study of the vibrational spectra of 12c4-alkali metal cation complexes was reported by Fukushima and Tamaki in 1987.<sup>40</sup> The authors reported the Raman spectra of the 12c4- $\text{Li}^+$ , - $\text{Na}^+$ , - $\text{K}^+$ , - $\text{NH}_4^+$ , - $\text{Mg}^{2+}$ , - $\text{Ca}^{2+}$ , - $\text{Sr}^{2+}$ , - $\text{Ba}^{2+}$ , and - $\text{Pb}^{2+}$  complexes in the region below 1000  $\text{cm}^{-1}$ . The assignment of the fundamental vibrations was aided by frequencies calculated using an empirical force field. The study predicted a  $D_{2d}$  structure of the 12c4- $\text{Li}^+$ , - $\text{Na}^+$ , - $\text{K}^+$ , - $\text{NH}_4^+$ , and - $\text{Mg}^{2+}$  complexes and a  $C_{2v}$  structure of the 12c4- $\text{Ca}^{2+}$ , - $\text{Sr}^{2+}$ , and - $\text{Ba}^{2+}$  complexes. This result contradicts an earlier



and  $C_4$ <sup>49</sup> conformations have been reported for the 12c4–Cu<sup>2+</sup>, –Mg<sup>2+</sup>, and –Ca<sup>2+</sup> complexes, respectively.

In view of these conflicting results about the conformation, or conformations, assumed by 12c4–alkali metal cation complexes and the absence of a detailed vibrational study of these complexes, it was felt that such a study would be necessary. This would be also in line with our previous studies of the conformational and vibrational analysis of crown ethers. The aim of the present report is then to measure the vibrational, Raman, and IR spectra of the five 12c4–alkali metal cation complexes. In addition, to compare between the experimental and calculated vibrational spectra of these complexes assuming any of the possible conformations of the complexes. This is in an effort to determine in which conformation these complexes exist in. Finally, aided by accurately calculated scale quantum mechanical (SQM) B3LYP force field, the fundamental vibrational frequencies of the complex are assigned.

### Experimental Details

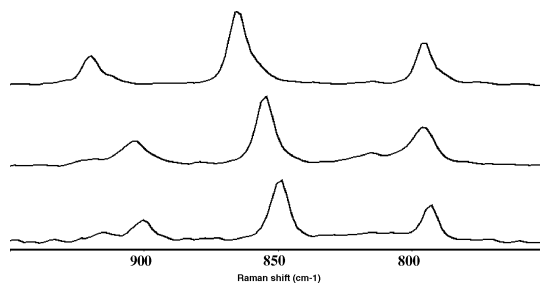
12c4–alkali metal cation complexes were synthesized by heating for 2 h, under reflux in methanol or in aqueous solution, a slight excess of an equimolar amount of the alkali metal chloride salts and 12c4.<sup>26</sup> The solvent was allowed to evaporate by placing the mixture in a closed desiccator under vacuum whereby crystals of the complex were formed. Some of the complexes were obtained in an emulsified form that did not form a precipitate. To these complexes, ether was added. Upon evaporation of the ether, crystals of the complexes were obtained.

FT-IR spectra were measured using a Thermo Nicolet Nexus 870 FT-IR instrument. The instrument uses a KBr beamsplitter and an InGaAs detector. Typically, between 128 or 256 scans were collected with a resolution of 1 cm<sup>-1</sup>. Solid samples were measured as KBr pellets. Solution samples, in methanol, were measured using a fixed path length cell equipped with KBr windows. The path length of the cell was varied using Teflon spacers of different thicknesses.

The FT-Raman spectra were measured using a Thermo Nicolet Nexus FT-Raman spectrometer. The instrument uses an air-cooled Nd:YVO<sub>4</sub> laser source which emits continuous-wave laser energy at a wavelength of 1064 nm, a XT-KBr beam-splitter, a 180° sample configuration and an InGaAs detector. Between 1024 and 4096 scans at a resolution of 4 cm<sup>-1</sup> were collected. To maximize the signal-to-noise ratio and due to the weak scattered light from the complex samples, a laser power of up to 1.0 W was used.

### Computational Details

Conformational analysis of the five 12c4–alkali metal cation complexes, to predict the possible conformations of the complexes, was reported in a previous publication.<sup>31</sup> Cartesian coordinate force fields were calculated, at the corresponding optimized geometries, for six of the eight predicted conformations. The other two conformations have  $C_1$  symmetry and were not considered. The six conformations considered have symmetries of, in energy order,  $C_4$ ,  $C_s$ ,  $C_s$ ,  $C_{2v}$ ,  $C_{2v}$ , and  $C_s$ , as detailed in ref 31. Notice that for the Li<sup>+</sup> complex in all levels considered in ref 31, except at the HF/3-21G level, the energy order of the first  $C_4$  and second  $C_s$  conformations is reversed and the third  $C_s$  conformation collapses to the second  $C_s$  conformation. The force fields were calculated at the B3LYP level due to its known excellent accuracy to CPU time ratio.<sup>50</sup> As was detailed in ref 31, the 6-31+G\* basis set was used for all atoms except for the K, Rb, and Cs atoms.<sup>31,51–56</sup> For these,



**Figure 4.** Raman spectra of the solid phase of the three 12c4–Li<sup>+</sup> (top), Na<sup>+</sup> (middle) and K<sup>+</sup> (bottom) complexes in the 950–750 cm<sup>-1</sup> region. The Figure shows a shift of the position of some bands of the 12c4–Li<sup>+</sup> complex compared to the corresponding bands of the Na<sup>+</sup> and K<sup>+</sup> complexes.

the Hay and Wadt's 10-valence-electron effective core potential (ECP) with a (5s4p)/[3s2p] valence basis set was used.<sup>57</sup> The basis set has an additional six-term  $d$ -type polarization functions with exponents of  $\alpha_d = 0.48$  for K,  $\alpha_d = 0.24$  for Rb, and  $\alpha_d = 0.19$  for Cs. For simplicity, this basis set will be termed the 6-31+G\* basis set. The additional diffuse function in the 6-31+G\* basis set was used to minimize the basis set superposition error and for its known necessity for accurate computation of the properties of the metal cation complexes. The basis set used for the K, Rb, and Cs atoms is the same as that used by Feller et al. for similar computations of 12c4– and 18c6–alkali metal cation complexes.<sup>33,37,38,61</sup>

All ab initio computations were performed using the Gaussian 98W<sup>62</sup> and Gaussian 03W<sup>63</sup> programs. The Gaussian program default parameters of geometry optimization and force field calculations were used. The force fields and dipole derivative tensors were calculated analytically. Since analytical polarizability derivatives are not available in the current version of the Gaussian program, these were calculated numerically.

The selection of the internal coordinates,<sup>64–66</sup> conversion of the Cartesian coordinate force fields to internal coordinate force fields,<sup>65,67</sup> scaling of the internal coordinate force fields<sup>65,68,69</sup> and refinement of the scale factors were done using the SCALE2 program<sup>70</sup> and were performed as was detailed elsewhere.<sup>25</sup> They are mentioned here for completeness. The SCALE2 program has the advantage of minimizing human interference and consequent error. In the first step of the program, from the frequency job archive of the Gaussian program output file, the program generates four files of the molecule Cartesian coordinates, Cartesian coordinate force field, dipole derivative tensors and polarizability derivatives. In the second step, the program generates the internal coordinates that are used to convert the Cartesian coordinate force field, dipole derivative tensors and polarizability derivatives to their internal coordinate counterparts. In the third step of the program, the internal coordinate force field is scaled according to the equation

$$F_{ij}^{\text{scaled}} = F_{ij}^{\text{theo}}(c_i c_j)^{1/2}$$

where  $c_i$  and  $c_j$  are the scale factors of the internal coordinates  $i$  and  $j$ , respectively. The reproducibility of the frequencies calculated by the Gaussian program is checked using a scale factor of 1.0. To aid in the initial assignment of the fundamental vibrations from the experimental spectra, the internal coordinate force fields are scaled with an initial scale factor of 0.963.<sup>71–73</sup> The experimental fundamental vibrations were then assigned to the calculated frequencies in frequency order taking into consideration the IR and Raman intensities. As the number of assigned bands increased, the number of scale factors was increased and the scale factors were varied, to minimize the

**TABLE 4: FT-Raman and FT-IR Frequencies (cm<sup>-1</sup>) and Assignment of 12c4–K<sup>+</sup> Complex<sup>a</sup>**

Raman			IR		assgnt
MeOH <sup>b</sup>		H <sub>2</sub> O <sup>c</sup> solid	MeOH <sup>b</sup>		
solid	MeOH		MeOH	solid	
140	136	141			<i>v</i> <sub>39</sub>
191	189	188			<i>v</i> <sub>60</sub>
	202				
208	217	212			( <i>v</i> <sub>38</sub> )
231	239	234			<i>v</i> <sub>19</sub>
269	264	265			<i>v</i> <sub>59</sub>
301	304	301			<i>v</i> <sub>18</sub>
343	349	344			<i>v</i> <sub>17</sub>
356	359	360			<i>v</i> <sub>58</sub>
375	376	376			
397	398				<i>v</i> <sub>37</sub>
429	425	413		419	
492	497	492			<i>v</i> <sub>36</sub>
				549	<i>v</i> <sub>57</sub>
599	597	600			<i>v</i> <sub>16</sub>
793	795	793		791	<i>v</i> <sub>35</sub>
808	804	810		808	<i>v</i> <sub>56</sub>
814	816				
849	848	849	848	846	<i>v</i> <sub>15</sub>
900	902	901			<i>v</i> <sub>34</sub>
915	910	914	916	913	<i>v</i> <sub>55</sub>
				1025	<i>v</i> <sub>13</sub>
1032		1030		1031	<i>v</i> <sub>54</sub>
1045		1045			<i>v</i> <sub>33</sub>
1059		1055			<i>v</i> <sub>12</sub>
1097	1097	1094		1094	<i>v</i> <sub>53</sub>
1116	1112	1115		1111	<i>v</i> <sub>11</sub>
1136	1138	1136		1134	<i>v</i> <sub>52</sub>
1162	1163	1162			<i>v</i> <sub>31</sub>
1238	1243	1237		1237	<i>v</i> <sub>10</sub>
			1250	1248	<i>v</i> <sub>51</sub>
1253	1256	1250			<i>v</i> <sub>29</sub>
				1254	<i>v</i> <sub>30</sub>
1267		1258		1259	
1278	1277	1278		1278	
1291	1292	1294	1291	1289	<i>v</i> <sub>50</sub>
1304	1304	1305	1306	1303	<i>v</i> <sub>9</sub>
1349	1353	1350		1348	<i>v</i> <sub>8</sub>
1368	1368	1371		1365	<i>v</i> <sub>49</sub>
1379	1377	1379		1378	<i>v</i> <sub>28</sub>
1392	1386	1391		1388	<i>v</i> <sub>7</sub>
1401	1400	1401		1399	<i>v</i> <sub>48</sub>
1410	1407	1410		1405	<i>v</i> <sub>27</sub>
				1449	<i>v</i> <sub>47</sub>
1450		1450			<i>v</i> <sub>26</sub>
				1467	<i>v</i> <sub>46</sub>
1471		1471		1472	<i>v</i> <sub>6</sub>
1485		1485		1483	<i>v</i> <sub>5</sub>
2871		2871		2865	
2886		2886		2882	
2906		2906		2908	
2929		2928		2926	
2938		2939		2934	
				2949	
				2956	

<sup>a,b,c</sup> See corresponding footnotes in Table 2.

difference between the calculated and experimental vibrational frequencies, as indicated by the rms deviation of the difference between the calculated and assigned experimental vibrational frequencies.

## Results and Discussion

### Structure of the 12c4—Alkali Metal Cation Complexes.

Figure 1 shows the structure and atom numbering of the *C*<sub>4</sub> conformation of the 12c4—alkali metal cation complex. Table 1 shows the geometry of this conformation at the B3LYP and MP2 levels using the 6-31+G\* basis set. The details of the MP2 computations are as given in ref 31. It can be noticed from the data in Table 1 that there is an increase of the displacement of the metal cation out of the ring plane, M—O bond length, where M refers to alkali metal cation, by the increase of the metal

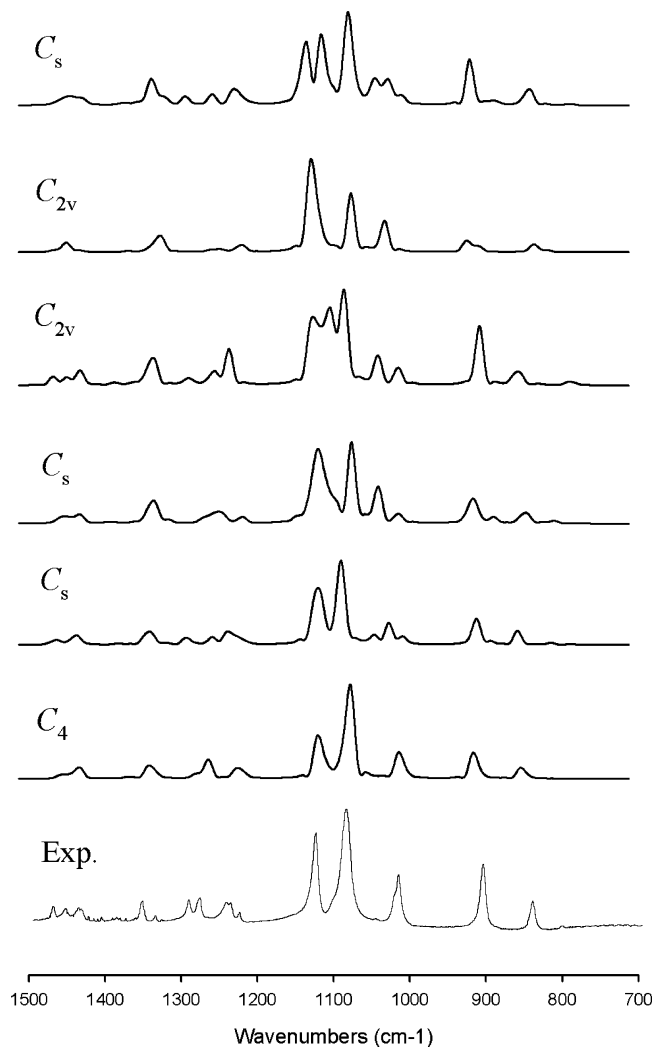
cation size. While the C—C bond length is unchanged for the five complexes, the C—O bond length of the Cs<sup>+</sup> complex is shorter by 0.01 Å than that of the Li<sup>+</sup> complex. Also, the two CCO bond angles increased by about 4 degrees. There is a large increase of the MO<sub>4</sub>C<sub>5</sub> bond angle by about 14 degrees, although the other MO<sub>4</sub>C<sub>3</sub> bond angle increased by less than 2 degrees. In addition, there is a large decrease of the MO<sub>1</sub>C<sub>2</sub>C<sub>3</sub> dihedral angle by about 20 degrees, as the large Cs<sup>+</sup> cation is displaced out of the ring plane compared to that of the smaller Li<sup>+</sup> cation. These previous differences are monotonic in going from the smallest Li<sup>+</sup> cation to the largest Cs<sup>+</sup> cation.

While the C—O bond lengths calculated at the MP2 and B3LYP levels are close to each other within 0.003 Å, the C—C bond lengths calculated at the B3LYP level are too short by not more than 0.01 Å, compared to those calculated at the MP2 level. The M—O bond length of the Li<sup>+</sup> complex is calculated to be equal at the MP2 and B3LYP levels, while for the Na<sup>+</sup> complex it is calculated to be too long by about 0.06 Å at the MP2 level compared to that at the B3LYP level. Using the effective core potential basis set for the K<sup>+</sup>, Rb<sup>+</sup>, and Cs<sup>+</sup> cations for the corresponding 12c4 complexes, the M—O lengths are calculated to be too short by about 0.06 Å at the B3LYP level compared to that at the MP2 level. There are two reports of the X-ray experimental geometry, to the best of our knowledge, of only the Na<sup>+</sup> complex.<sup>45,46</sup> The calculated geometries at the B3LYP and MP2 levels in Table 1 are in good agreement with these X-ray experimental geometries.

**Experimental Vibrational Spectra of the 12c4—Alkali Metal Cation Complexes.** The Raman spectra in the 100–1600 cm<sup>-1</sup> region of the Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> complexes in the solid phase and the IR spectra in the 400–1600 cm<sup>-1</sup> region of the five 12c4—alkali metal cation complexes of the solid phase are shown in Figures 2 and 3, respectively. No reasonable Raman spectra could be obtained for the Rb<sup>+</sup> and Cs<sup>+</sup> complexes, even using samples synthesized using either methanol or water as a solvent, as will be detailed shortly. Tables 2–4 list the Raman vibrational frequencies of the solid and methanol solution phases of the Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> complexes, in addition to the Raman frequencies of the water solution phase of the Li<sup>+</sup> and Na<sup>+</sup> complexes. The IR vibrational frequencies of the three Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> complexes of the solid phase are also added in Table 3. The assignment of the fundamental vibrations is included in Tables 2–4. The Raman vibrational frequencies of the methanol solution reported in ref 40 are added in Tables 2 and 3 for the Li<sup>+</sup> and Na<sup>+</sup> complexes, respectively.

It has been reported that the solvent used in the synthesis of the crown ether—metal complexes affects the stability of the formed complexes.<sup>26</sup> In the current study, the complexes were synthesized using methanol as a solvent. To study the effect of the solvent used in the synthesis of the complexes, the Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> complexes were also synthesized using water as a solvent. The Raman vibrational frequencies of the aqueous phase of the Li<sup>+</sup> complex, the solid and aqueous phase of the Na<sup>+</sup> complex and the solid phase of the K<sup>+</sup> complex are included in Table 2. In addition, the IR vibrational frequencies of the solid and methanol solution phases of the Na<sup>+</sup> complex are added to Table 3. In the IR spectra of the Na<sup>+</sup> complex of the solid phase, Table 3, the difference between the frequencies of the corresponding bands, when methanol and water were used as solvents in the synthesis of the complex, is about 1 or 2 cm<sup>-1</sup>, but it can be as large as 6 cm<sup>-1</sup> for very weak bands. For the Raman spectra of the solid phase, the difference is also 1 or 2 cm<sup>-1</sup>, but for some bands, the difference is as large as 6 cm<sup>-1</sup>, such as for *v*<sub>29</sub>. These small band position differences in the





**Figure 6.** Experimental and calculated IR spectra of the 12c4–K<sup>+</sup> complex using unscaled frequencies.

It is clear from Figures 2 and 3 that the vibrational spectra of the five 12c4–alkali metal cation complexes are so similar that it is reasonable to conclude that the five complexes exist in the same conformation. As will be seen shortly, it is concluded that the five complexes exist in the  $C_4$  conformation. There is a shift of the position of some bands of the Li<sup>+</sup> complex, compared to those of the other four complexes. Figure 4 compares between the Raman spectra of the solid phase of the 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> complexes in the region of 950–750 cm<sup>-1</sup>. For example,  $\nu_{55}$  of the 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> complexes is at 931, 918, and 915 cm<sup>-1</sup>, respectively, while  $\nu_{56}$  of the same complexes is at 802, 802, and 808 cm<sup>-1</sup>, respectively. The shift of the position of some bands of the Li<sup>+</sup> complex is not necessarily toward higher energy. For example,  $\nu_{53}$  of the 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> complexes is at 1082, 1098, and 1095 cm<sup>-1</sup>, respectively.

The similarity between the vibrational spectra of the five 12c4–alkali metal cation complexes, as presented by the data in Figures 2 and 3 and Tables 2–4, suggests that the five alkali metal cation complexes exist in the same conformation. Comparison was made between the experimental and calculated vibrational frequencies for six of the eight predicted conformations reported in ref 31 of the 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> complexes that are of symmetries higher than the  $C_1$  symmetry. These six conformations, in energy order, are of  $C_4$ ,  $C_s$ ,  $C_s$ ,  $C_{2v}$ ,  $C_{2v}$ , and  $C_s$  symmetries. Because of the doubly degenerate

$E$  representation of the  $C_4$  point group, the comparison concludes that the three complexes exist in the  $C_4$  conformation. Table 5 shows such comparison for the 12c4–K<sup>+</sup> complex. The vibrational frequencies are scaled with a one frequency scale factor of 0.963.<sup>71</sup> Although no Raman spectra could be obtained for the Rb<sup>+</sup> and Cs<sup>+</sup> complexes, the similarity between the IR spectra of the five complexes clearly shows that the five complexes exist in the same conformation. The existence of the five complexes in the  $C_4$  conformation is a reflection of the fact that the five alkali metal cations are larger than the ring cavity of 12c4. Scaling of the force field was then conducted using the B3LYP/6-31+G\* force field of the  $C_4$  conformation. The conclusion that the Na<sup>+</sup> complex has a  $C_4$  structure is in agreement with X-ray result that this complex exists in the  $C_4$  conformation.<sup>45,46</sup> This is the only complex of the 12c4–alkali metal cation complexes for which, to the best of our knowledge, an X-ray result has been reported. Figures 5 and 6 compare between the experimental and calculated Raman and IR, respectively, spectra of the 12c4–K<sup>+</sup> complex. Because of an unsolved problem in the computations, no Raman intensities were calculated for the third lowest  $C_s$  conformation. Both figures, Figures 5 and 6, show a better agreement between the experimental and calculated Raman and IR spectra assuming a  $C_4$  conformation of the complex.

Table 6 compares between the calculated, unscaled, vibrational frequencies of the five 12c4–alkali metal cation complexes of the  $C_4$  conformation. The data in Table 6 reflect the similarity between the calculated vibration spectra of the five complexes as observed experimentally, Figures 2 and 3 and Tables 2–4. This is only with the exception of the region below 400 cm<sup>-1</sup>. This region is characterized by the vibrational modes involving the alkali metal cation, where the difference between the calculated geometries of the five alkali metal cations, described before, is reflected by the difference between the calculated spectra in this region. For example, for the 12c4–K<sup>+</sup> complex, the calculated TED shows a large contribution of the K<sup>+</sup>–O stretching mode for the  $\nu_{18}$ ,  $\nu_{20}$ ,  $\nu_{38}$ ,  $\nu_{39}$ ,  $\nu_{59}$ , and  $\nu_{61}$  vibrational modes. Notice also that these bands, compared to the other intense bands, are of modest intensity to have a significant influence on the measured experimental vibrational spectra.

**Scaling of the Force Fields of the  $C_4$  Conformation.** 12c4–alkali metal cation complexes are large ring molecules with 81 normal modes of vibration. While free 12c4 has no redundant internal coordinates,<sup>25</sup> due to symmetry and the additional alkali metal cation, 12c4–alkali metal cation complexes have 90 redundant internal coordinates that were generated by the SCALE2 program. This set of 90 internal coordinates was reduced to 81 nonredundant internal coordinates. The nine vibrations corresponding to the redundant coordinates were calculated to be zero. A set of eight scale factors were used in the scaling of the force fields. The values of the scale factors were estimated after comparison between those determined for free 12c4<sup>25</sup> and those determined by Rauhut and Pulay as average scale factors of a set of 20 molecules.<sup>71</sup> Using this initial set of scale factors, without varying the scale factors, the rms deviations of the difference between the calculated and experimental vibrational frequencies for the Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> complexes were 11.0, 6.4, and 5.9 cm<sup>-1</sup>, respectively.

The definition of the internal coordinates, used in the conversion of the internal coordinate force fields to the Cartesian coordinate force fields, the initial and final values of the eight scale factors of the force fields of the three 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> cation complexes, and the corresponding rms devia-

**TABLE 6: Comparison between the Calculated, Unscaled, Vibrational Frequencies (cm<sup>-1</sup>) and IR and Raman Intensities for the Five 12c4–Alkali Metal Cation Complexes of the C<sub>4</sub> Conformation<sup>a</sup>**

no.	sym.	Li <sup>+</sup>			Na <sup>+</sup>			K <sup>+</sup>			Rb <sup>+</sup>			Cs <sup>+</sup>	
		freq	IR	Ra	freq	IR	Ra	freq	IR	Ra	freq	IR	Ra	freq	IR
1	A	3141	24	38	3129	37	46	3120	58	48	3116	69	49	3112	79
2		3087	0	308	3079	5	91	3077	13	50	3075	16	59	3072	18
3		3079	6	313	3067	15	539	3056	24	637	3051	29	651	3045	35
4		3037	82	226	3039	68	199	3034	54	148	3030	50	129	3024	48
5		1542	12	9	1539	11	11	1539	9	13	1540	8	13	1540	7
6		1512	1	9	1511	2	11	1510	3	12	1510	3	13	1509	3
7		1432	0	1	1434	0	1	1432	1	1	1434	2	1	1434	2
8		1385	2	2	1388	2	2	1389	2	2	1390	2	2	1391	2
9		1327	18	4	1333	20	4	1335	21	5	1337	20	5	1339	21
10		1256	6	5	1263	4	4	1264	4	4	1266	5	4	1267	5
11		1136	5	3	1133	0	1	1141	0	2	1144	0	2	1148	0
12		1057	5	0	1060	0	4	1057	0	4	1057	0	4	1058	0
13		1026	63	1	1032	72	1	1036	76	1	1038	77	1	1039	79
14		920	0	0	915	0	7	912	0	8	910	0	8	910	0
15		871	33	20	861	38	17	857	43	15	854	44	14	854	46
16		603	2	3	596	1	3	592	1	3	593	1	3	593	0
17		384	44	5	354	9	4	344	8	2	340	7	1	337	0
18		322	31	1	310	1	2	292	0	3	289	0	3	287	7
19		311	0	0	244	6	1	243	2	0	247	1	0	247	1
20		205	0	1	195	22	0	155	21	0	110	10	0	88	7
21	B	3140	0	40	3128	0	39	3119	0	39	3115	0	39	3110	0
22		3086	0	66	3074	0	56	3066	0	42	3062	0	35	3057	0
23		3076	0	115	3062	0	97	3050	0	86	3046	0	81	3039	0
24		3024	0	28	3026	0	50	3024	0	82	3023	0	96	3018	0
25		1525	0	2	1517	0	2	1515	0	1	1513	0	2	1513	0
26		1511	0	27	1509	0	27	1509	0	27	1508	0	26	1507	0
27		1436	0	1	1440	0	0	1442	0	0	1444	0	0	1445	0
28		1418	0	2	1420	0	3	1422	0	4	1422	0	4	1423	0
29		1287	0	10	1293	0	26	1297	0	33	1300	0	34	1301	0
30		1275	0	19	1286	0	6	1287	0	2	1289	0	1	1289	0
31		1173	0	2	1177	0	2	1180	0	2	1181	0	2	1181	0
32		1128	0	1	1132	0	3	1133	0	3	1135	0	3	1137	0
33		1064	0	3	1062	0	0	1068	0	0	1071	0	0	1073	0
34		928	0	7	915	0	0	916	0	0	915	0	1	916	0
35		782	0	8	786	0	9	792	0	9	793	0	9	795	0
36		496	0	4	493	0	4	490	0	4	488	0	3	487	0
37		403	0	0	409	0	0	406	0	0	406	0	0	406	0
38		234	0	0	216	0	0	202	0	0	198	0	0	194	0
39		171	0	0	159	0	0	140	0	0	136	0	0	136	0
40		108	0	0	124	0	0	117	0	0	112	0	0	103	0
41		63	0	0	69	0	1	56	0	1	47	0	1	45	0
42	E	3140	5	93	3129	8	91	3119	14	88	3115	17	86	3111	19
43		3086	63	20	3075	65	44	3069	57	61	3067	51	63	3062	46
44		3077	13	23	3064	31	30	3053	61	33	3048	79	37	3042	94
45		3030	2	4	3033	3	2	3030	5	4	3027	6	7	3021	7
46		1532	12	6	1525	12	4	1524	11	4	1523	11	4	1524	11
47		1511	14	1	1510	14	1	1509	14	1	1509	13	1	1508	12
48		1436	1	1	1438	2	1	1438	2	1	1440	3	2	1441	3
49		1402	27	0	1405	29	0	1406	31	1	1407	32	1	1408	33
50		1314	30	7	1320	28	6	1321	27	7	1323	25	7	1324	25
51		1263	24	1	1273	24	1	1276	24	2	1279	24	2	1280	24
52		1154	55	1	1154	69	1	1156	88	1	1157	98	2	1159	108
53		1102	245	4	1108	215	3	1113	187	2	1116	175	2	1118	162
54		1037	21	3	1039	16	2	1041	14	2	1042	13	2	1043	12
55		943	43	0	930	50	0	927	49	0	925	50	0	925	48
56		810	1	0	810	0	0	812	0	0	812	0	0	814	0
57		559	18	0	551	13	0	548	12	0	549	12	0	549	12
58		439	78	0	409	0	0	406	0	0	406	0	0	406	0
59		351	6	0	290	14	0	269	5	0	264	4	0	260	3
60		286	3	0	214	20	0	191	18	0	193	16	0	192	16
61		176	9	0	183	1	0	127	9	0	94	5	0	75	4

<sup>a</sup> IR and Ra are the IR and Raman intensities, respectively. No Raman intensity was calculated for the Cs<sup>+</sup> complex.

tions are given in Table 7. Since none of the vibrations corresponding to the C–H stretching mode and most of the vibrations involving the Na butterfly mode were not assigned, the scale factors corresponding to the C–H stretching and Na butterfly modes were held fixed. The total number of the experimental frequencies used in the determination of the final

scale factors are 50, 60, and 56 vibrational frequencies for the 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> complexes, respectively.

The experimental vibrational frequencies used in the scaling of the force fields and the corresponding calculated vibrational frequencies and Raman and IR intensities of the C<sub>4</sub> conformation of three 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> cation complexes are given



**TABLE 7: Natural Internal Coordinate Scale Factors<sup>a</sup>**

coordinate	description	initial	final		
			Li <sup>+</sup>	Na <sup>+</sup>	K <sup>+</sup>
$R_1-R_4$	C–C stretching	0.970	0.9858	0.9977	0.9785
$R_5-R_{12}$	C–O stretching	1.022	1.0013	1.0106	1.0092
$R_{13}$	M–O stretching	0.940	0.8927	0.8477	1.0900
$r_{13}-r_{28}$	C–H stretching <sup>b</sup>	0.920	0.9200	0.9200	0.9200
$\alpha_1-\alpha_{32}$	CH <sub>2</sub> bending	0.940	0.9454	0.9417	0.9391
$\zeta_1-\zeta_9$	ring bending <sup>c</sup>	1.040	1.0426	1.0130	1.0494
$\tau_1-\tau_9$	ring Torsion	1.030	0.8968	1.0634	0.9784
$\tau_{10}$	MO butterfly <sup>b</sup>	0.940	0.9400	0.9400	0.9400
rms			7.7	5.6	5.1

<sup>a</sup> Nonredundant internal coordinates. M refers to alkali metal cation.

<sup>b</sup> Fixed. See text. <sup>c</sup> Including those which contain the M metal cation.

in Tables 8–10. Bands for which their assignments as fundamental was not certain, and were consequently not used in the scaling of the force fields, are included between parentheses in Tables 8–10. In the scaling of the force fields, the experimental vibrational frequencies of the methanol solution, whenever available, were used, in most of the cases. Since the vibrational spectra of the three 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> complexes are quite similar, Figures 2 and 3, the assignment of the experimental to the calculated vibrational frequencies was revised so that the same strong features in the spectra of the three complexes would correspond to the same mode in the calculated spectra.

A few remarks should be mentioned about the assignment of the experimental to the calculated vibrational frequencies for the three 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> complexes. Except for  $\nu_{17}$  and  $\nu_{19}$  of the Li<sup>+</sup> complex and  $\nu_{17}$  and  $\nu_{18}$  of the Na<sup>+</sup> and K<sup>+</sup> complexes, which are observed as strong bands in the Raman spectra at about 350 and 305 cm<sup>-1</sup>, respectively, most of the other vibrational bands in the 150–400 cm<sup>-1</sup> region are very weak and difficult to assign. In addition, only Raman spectral data are available in this region. Bands in the 100–150 cm<sup>-1</sup> region are also broad and due to the overlap of bands in this region are not possible to assign. In the vibrational spectra of the 12c4–Na<sup>+</sup> complex, three bands are observed in the 790–820 cm<sup>-1</sup> region, although, using the scaled force field, two bands are predicted to be in this region. The band observed at 794 cm<sup>-1</sup> was selected as a fundamental since it is observed and predicted as intense band in the Raman spectra. Two other bands are observed at 802 and 814 cm<sup>-1</sup>. The 802 cm<sup>-1</sup> band was selected, rather than the 814 cm<sup>-1</sup> band, as a fundamental in agreement with the scaled B3LYP vibrational frequency, at 800 cm<sup>-1</sup>. The 1340–1500 cm<sup>-1</sup> region is the most difficult region to assign. It can be divided into two regions, the first is at 1340–1410 cm<sup>-1</sup> and the second is at 1440–1500 cm<sup>-1</sup>. Either region has six bands, two of which are of *E* symmetry. It was easier to assign the second 1440–1500 cm<sup>-1</sup> region, but the difference between the calculated, using the scaled B3LYP force field, and experimental frequencies in this region was as high as 21 cm<sup>-1</sup>. On the other hand, it was not simple to assign the first 1340–1410 cm<sup>-1</sup> region, especially since some bands were weak. Consequently, two calculated bands were preferred to be left unassigned in this region.

For the three 12c4–Li<sup>+</sup>, –Na<sup>+</sup>, and –K<sup>+</sup> complexes, the values of the scale factors corresponding to the C–C stretching, C–O stretching, and CH<sub>2</sub> bending modes, Table 7, are close to each other, within 0.02 at the highest, and those of the ring bending mode are close to each other, within 0.04. For the M–O stretching mode, the values of the scale factors for the three complexes are different, within 0.24, although this can be rationalized in large part due to the three different M alkali metal cations, Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup>. The values of the scale factors

**TABLE 8: Experimental and Calculated Vibrational Frequencies (cm<sup>-1</sup>) and Raman and IR Intensities ((4 $\pi\epsilon_a$ )<sup>2</sup> Å<sup>4</sup> amu<sup>-1</sup>) of the C<sub>4</sub> Conformation of the 12c4–Li<sup>+</sup> Complex<sup>a</sup>**

no.	sym	exptl freq	calcd			
			freq	IR int	Raman int depo	
1	A		3016	23.9	37.9	0.07
2			2964	0.4	307.0	0.15
3			2957	6.2	314.2	0.01
4			2916	82.5	225.6	0.00
5		1499	1499	11.8	8.7	0.75
6			1470	1.3	8.7	0.64
7			1400	0.0	1.3	0.04
8		1350	1345	2.1	2.2	0.32
9		1289	1292	18.7	3.9	0.27
10		1241	1222	6.7	5.2	0.36
11		1113	1112	7.8	3.1	0.00
12		1048	1048	1.3	0.2	0.75
13		1020	1020	64.5	1.3	0.00
14		907	908	1.2	0.4	0.18
15		862	865	27.7	20.1	0.07
16		603	605	1.3	2.2	0.10
17		351	362	45.5	5.0	0.00
18		324	320	32.0	1.4	0.08
19		305	298	0.2	0.2	0.26
20		(199)	199	0.1	0.7	0.08
21	B		3015	0.0	40.5	0.75
22			2963	0.0	66.1	0.75
23			2954	0.0	114.6	0.75
24			2903	0.0	28.2	0.75
25		1479	1482	0.0	2.3	0.75
26		1454	1468	0.0	26.9	0.75
27			1400	0.0	1.3	0.75
28			1378	0.0	1.9	0.75
29			1255	0.0	10.1	0.75
30		1261	1241	0.0	18.5	0.75
31		1159	1146	0.0	3.6	0.75
32		1120	1123	0.0	1.0	0.75
33		1059	1057	0.0	2.7	0.75
34		917	918	0.0	7.7	0.75
35		786	771	0.0	7.6	0.75
36		500	501	0.0	4.3	0.75
37		(400)	393	0.0	0.1	0.75
38		(229)	232	0.0	0.3	0.75
39		(158)	164	0.0	0.3	0.75
40			104	0.0	0.2	0.75
41			60	0.0	0.5	0.75
42	E		3015	5.2	93.2	0.75
43			2963	63.1	19.6	0.75
44			2955	13.3	22.8	0.75
45			2909	2.1	4.4	0.75
46		1487	1489	11.8	5.8	0.75
47		1446	1469	13.7	1.3	0.75
48			1398	1.1	1.0	0.75
49		1360	1362	26.6	0.2	0.75
50		1277	1281	34.2	6.6	0.75
51		1252	1229	29.5	1.3	0.75
52		1137	1131	119.1	2.0	0.75
53		1083	1092	175.3	2.7	0.75
54		1027	1030	21.1	2.7	0.75
55		931	934	41.1	0.3	0.75
56		802	799	0.2	0.0	0.75
57		562	563	20.3	0.1	0.75
58		415	413	73.4	0.2	0.75
59		341	345	4.3	0.0	0.75
60		282	281	4.8	0.1	0.75
61		(167)	170	9.5	0.1	0.75

<sup>a</sup> Here, sym, exptl, calcd, freq, int, and depo stand for symmetry, experimental, calculated, frequency, intensity and depolarization ratio, respectively. For the bands in parentheses, their assignment as fundamentals was not certain, and they were not used in the scaling of the force field.

corresponding to the ring torsion mode are also different, within 0.17. Notice that in the vibrational analysis of free 12c4, for most of the conformations considered in that study, a value of about 1.05 was obtained for the scale factor corresponding to the same ring torsion internal coordinate.<sup>25</sup> This value of 1.05 is the closest to that of the Na<sup>+</sup> complex, in the current study,

**TABLE 9: Experimental and Calculated Vibrational Frequencies ( $\text{cm}^{-1}$ ) and Raman and IR Intensities ( $(4\pi\epsilon_0)^2 \text{\AA}^4 \text{amu}^{-1}$ ) of the  $C_4$  Conformation of the 12c4-Na<sup>+</sup> Complex<sup>a</sup>**

no.	sym	exptl freq	calcd			
			freq	IR int	Raman	
					int	depo
1	A		3005	37.3	46.1	0.03
2			2956	4.8	91.0	0.47
3			2945	14.9	540.4	0.00
4			2918	67.6	197.5	0.01
5		1486	1494	11.0	11.2	0.75
6		1453	1467	2.0	10.5	0.66
7		(1396)	1396	0.2	1.1	0.05
8		1354	1348	3.1	2.2	0.39
9		1305	1297	21.2	3.9	0.35
10		1237	1227	5.3	4.3	0.35
11		1115	1118	8.7	3.0	0.00
12		1064	1057	0.7	0.2	0.32
13		1028	1028	70.7	1.63	0.01
14		895	899	0.2	0.3	0.71
15		852	861	34.2	16.1	0.07
16		601	594	1.2	3.1	0.08
17		347	352	9.9	2.9	0.00
18		302	300	0.3	3.1	0.04
19		248	248	7.6	0.5	0.01
20		196	191	20.4	0.1	0.64
21	B		3004	0.0	38.7	0.75
22			2952	0.0	55.7	0.75
23			2940	0.0	97.1	0.75
24			2905	0.0	50.0	0.75
25		1470	1473	0.0	1.7	0.75
26		1444	1465	0.0	26.7	0.75
27		(1400)	1399	0.0	0.3	0.75
28		1380	1378	0.0	2.7	0.75
29		1268	1258	0.0	27.5	0.75
30		1256	1251	0.0	3.5	0.75
31		1160	1158	0.0	3.5	0.75
32		1124	1133	0.0	1.1	0.75
33		1049	1051	0.0	3.4	0.75
34		906	907	0.0	7.8	0.75
35		794	777	0.0	8.5	0.75
36		494	494	0.0	3.6	0.75
37		(414)	410	0.0	0.1	0.75
38		204	210	0.0	0.2	0.75
39		148	155	0.0	0.5	0.75
40		(131)	121	0.0	0.1	0.75
41			71	0.0	0.8	0.75
42	E		3004	8.4	91.5	0.75
43			2953	64.8	43.4	0.75
44			2942	31.4	29.8	0.75
45			2912	3.1	2.0	0.75
46		1476	1480	11.7	4.2	0.75
47		1447	1466	13.4	1.0	0.75
48		1410	1399	2.2	1.2	0.75
49		1365	1363	27.5	0.4	0.75
50		1290	1284	35.1	5.9	0.75
51		1248	1239	31.6	1.4	0.75
52		1138	1140	145.9	2.4	0.75
53		1098	1100	132.8	1.8	0.75
54		1033	1033	14.3	2.3	0.75
55		918	920	45.0	0.3	0.75
56		802	800	0.1	0.2	0.75
57		553	552	12.9	0.1	0.75
58		368	364	6.6	0.1	0.75
59		285	282	10.8	0.0	0.75
60		215	215	25.9	0.2	0.75
61		181	182	0.1	0.0	0.75

<sup>a</sup> See corresponding footnote in Table 6.

which has the largest number of bands corresponding to the ring torsion mode assigned. This value of 1.05 is most different from that of the Li<sup>+</sup> complex. In a different calculation the scale factors of the Li<sup>+</sup> complex were varied after all of the low energy vibrational bands whose assignment as fundamentals were not certain, and thus are included between parentheses in Table 9, were included in the refinement of the scale factors. The rms deviation became better, 6.8  $\text{cm}^{-1}$ , but the values of the scale factors were close to those in Table 7, within 0.004.

**TABLE 10: Experimental and Calculated Vibrational Frequencies ( $\text{cm}^{-1}$ ) and Raman and IR Intensities ( $(4\pi\epsilon_0)^2 \text{\AA}^4 \text{amu}^{-1}$ ) of the  $C_4$  Conformation of the 12c4-K<sup>+</sup> Complex<sup>a</sup>**

no.	sym	exptl freq	calcd			
			freq	IR int	Raman	
					int	depo
1	A		2996	58.1	47.7	0.02
2			2954	13.1	50.3	0.61
3			2934	23.8	637.0	0.01
4			2913	53.9	148.2	0.03
5		1485	1491	8.4	13.3	0.75
6		1471	1464	2.9	11.8	0.67
7		1386	1392	1.1	1.4	0.04
8		1348	1347	3.8	2.8	0.38
9		1306	1297	22.5	4.4	0.36
10		1237	1226	5.1	4.3	0.31
11		1116	1118	7.9	2.7	0.00
12		1059	1056	1.8	0.4	0.05
13		1024	1029	76.0	1.7	0.02
14			902	0.0	0.4	0.72
15		848	852	36.9	14.3	0.07
16		597	592	0.7	2.9	0.09
17		349	344	7.9	2.6	0.00
18		304	297	0.4	2.2	0.07
19		239	240	2.0	0.5	0.02
20			159	20.9	0.1	0.51
21	B		2995	0.0	39.3	0.75
22			2944	0.0	42.3	0.75
23			2929	0.0	86.2	0.75
24			2903	0.0	81.7	0.75
25			1468	0.0	1.8	0.75
26		1450	1463	0.0	26.3	0.75
27		1407	1398	0.0	0.3	0.75
28		1377	1378	0.0	3.6	0.75
29		1254	1259	0.0	34.2	0.75
30		1250	1251	0.0	0.7	0.75
31		1162	1158	0.0	3.4	0.75
32			1138	0.0	1.7	0.75
33		1045	1048	0.0	3.6	0.75
34		902	898	0.0	8.1	0.75
35		795	782	0.0	8.8	0.75
36		497	497	0.0	3.5	0.75
37		398	403	0.0	0.2	0.75
38		(217)	208	0.0	0.1	0.75
39		140	141	0.0	0.4	0.75
40			115	0.0	0.1	0.75
41			56	0.0	1.0	0.75
42	E		2995	13.6	88.1	0.75
43			2947	57.0	60.6	0.75
44			2931	61.7	32.8	0.75
45			2909	4.6	3.8	0.75
46		1467	1477	11.0	3.8	0.75
47		1449	1463	12.8	0.9	0.75
48		1400	1397	2.4	1.3	0.75
49		1365	1362	29.2	0.6	0.75
50		1291	1284	35.6	6.3	0.75
51		1250	1239	33.1	2.0	0.75
52		1134	1141	177.2	2.9	0.75
53		1094	1100	88.2	1.1	0.75
54		1030	1033	14.9	2.3	0.75
55		913	914	43.7	0.3	0.75
56		808	803	0.2	0.2	0.75
57		549	551	11.1	0.2	0.75
58		359	360	6.5	0.1	0.75
59		269	272	6.0	0.1	0.75
60		189	188	17.0	0.0	0.75
61			130	8.8	0.2	0.75

<sup>a</sup> See corresponding footnote in Table 6.

It is reasonable then to assume that the values of the scale factor corresponding to the ring torsion mode of the Li<sup>+</sup> complex are not in error. In addition, this difference in the values of the scale factor, between that of the Li<sup>+</sup> and Na<sup>+</sup> complexes, is most probably too large to be attributable to a wrong assignment.

The rms deviation, of the difference between the experimental and calculated vibrational frequencies, of the Li<sup>+</sup> complex is higher than that of the other two Na<sup>+</sup> and K<sup>+</sup> complexes, Table 7. This larger rms deviation of the Li<sup>+</sup> complex is attributed

mainly to seven bands, out of the 50 bands assigned for this complex. In a different calculation, these seven bands were excluded from the assignment. The rms deviation became  $4.1 \text{ cm}^{-1}$  and the values of the scale factors were almost unchanged, within 0.009, including that of the ring torsion mode. Since the assignment of these seven bands was reliable, they were included in the final calculations, as presented in Table 8.

**Relative Energies of the  $C_4$  and  $C_s$  Conformations of the  $\text{Li}^+$  Complex.** The vibrational study preformed in this report predicts a  $C_4$  structure of the  $12c4\text{-Li}^+$  complex, as well as for the other four alkali metal cation complexes. As was mentioned above, in the previous conformational analysis report of the  $12c4\text{-alkali metal cation complexes}$ ,<sup>31</sup> the  $C_4$  conformation was predicted to be the most stable conformation for the four  $12c4\text{-Na}^+$ ,  $\text{-K}^+$ ,  $\text{-Rb}^+$ , and  $\text{-Cs}^+$  complexes. For the  $12c4\text{-Li}^+$  complex, a  $C_s$  conformation was calculated to be more stable than the  $C_4$  conformation by 0.16 kcal/mol at the MP2/6-31+G\* level. The calculated binding energy predict a  $C_4$  or  $C_s$  conformation of the  $12c4\text{-Li}^+$  complex but could not differentiate whether the complex exists in the  $C_4$  or  $C_s$  conformation. This is because the calculated binding energies of the  $C_4$  and  $C_s$  conformations are too close to each other,  $-93.0$  and  $-89.9$  kcal/mol, at the MP2/6-31+G\* level, respectively. This is accompanied by a large uncertainty of the experimental binding energy,  $-90 \pm 12$  kcal/mol. To further clarify whether the  $C_4$  or  $C_s$  conformation is the more stable conformation of the  $12c4\text{-Li}^+$  complex, optimized geometry of the complex was calculated for the  $C_4$  and  $C_s$  conformations at the MP2/6-311++G\*\* level. The MP2 computations were performed with the fixed core option. The  $C_4$  conformation was calculated to be more stable by 0.13 kcal/mol than the  $C_s$  conformation. This is compared to an energy difference of 0.16 kcal/mol at the MP2/6-31+G\* level, with the  $C_s$  conformation being more stable than the  $C_4$  conformation. These energy differences, at either the MP2/6-31+G\* or MP2/6-311++G\*\* level, are too small compared to the forces which are experienced in the solid or the solution phase. It is then concluded that other forces in the solid or the solution phase are the stabilizing force of the  $C_4$  conformation over the  $C_s$  conformation for the  $\text{Li}^+$  complex.

## Conclusion

This is the first time, to the best of our knowledge, that a full and detailed vibrational analysis of the spectra of any of the five  $12c4\text{-alkali metal cation complexes}$  is reported. The similarity between the measured vibrational spectra of the five complexes indicates that the five  $12c4\text{-alkali metal cation complexes}$  exist in the same conformation. Comparison between the experimental and calculated vibrational frequencies of the possible conformations of the  $12c4\text{-alkali metal cation complexes}$ , predicted in a previous conformational analysis study,<sup>31</sup> indicates that the five  $12c4\text{-alkali metal cation complexes}$  exist in the  $C_4$  conformation. This conclusion is in agreement with the previous conformational analysis study that the  $C_4$  conformation is the lowest energy conformation of the  $12c4\text{-Na}^+$ ,  $\text{-K}^+$ ,  $\text{-Rb}^+$ , and  $\text{-Cs}^+$  complexes. For the  $\text{Li}^+$  complex, the  $C_s$  conformation was calculated to be more stable than the  $C_4$  conformation by only 0.16 kcal/mol, at the MP2/6-31+G\* level.<sup>31,61</sup> To further investigate this point, optimized geometries were calculated, in the present work, for the  $C_s$  and  $C_4$  conformations of the  $\text{Li}^+$  complex at the MP2/6-311++G\*\* level. The  $C_4$  conformation was calculated to be more stable than the  $C_s$  conformation by 0.13 kcal/mol.

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